

MIDTERM REVIEW STUDY GUIDE

1. Locus Definition

$$y = \pm \frac{1}{4p}(x - h)^2 + k$$

Vertex: (h, k) (located in the middle of the focus (point) and directrix (line))

p = half the distance between directrix and focus

When you draw the parabola, remember it "eats the focus"

2. Average Rate of Change

$$\frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$

3. Exponent Rules

a) When multiplying, add exponents

b) When dividing, subtract exponents

c) Power to a Power $(2x^4y^2)^3 = 2^3x^{12}y^6 = 8x^{12}y^6$

Distribute (multiply) outside exponent to all inside exponents

c) To turn a radical into an exponent: $\frac{\text{power}}{\text{root}} \quad \sqrt{x} = x^{\frac{1}{2}}$

4. Functions

a) Even functions are symmetric to y-axis

b) Odd functions are symmetric to the origin

c) Transformations of Functions: in () effects the x values (shifts left/right or $r_{y\text{-axis}}$) outside parentheses effects the y-values (shifts up/down or $r_{x\text{-axis}}$)

5. Solving Equations

a) Factor: (GCF, DOTS, Trinomials, AC Method, Grouping, Cubes (SOAP))

b) Quadratic Formula (On reference sheet)

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

**Use when you can't factor a quadratic (x^2 function)

**Use when it says find the roots/zeros in simplest radical form or simplest "a + bi" form

c) Solving Radical Equations (Isolate radical, square both sides, solve & check)

MIDTERM REVIEW STUDY GUIDE

6. Sequences and Series Formulas (on reference sheet)

- a) Arithmetic Sequence: $a_n = a_1 + (n - 1)d$
- b) Geometric Sequence: $a_n = a_1 r^{n-1}$
- c) Geometric Series: $S_n = \frac{a_1 - a_1 r^n}{1-r}$
- d) Arithmetic Series: $S_n = \frac{n(a_1 + a_n)}{2}$ (**not on reference sheet**)
- e) Arithmetic Recursive Form: $a_n = a_{n-1} + d$
- f) Geometric Recursive Form: $a_n = r \cdot a_{n-1}$
- g) Sigma Notation/Summation: \sum

7. Exponential Functions:

- a) Writing the equation in $y = a(b)^x$ form;

a = y-intercept b = rate (multiplier)

Find b first: Divide the x's and y's
Work backwards on chart to find the y-intercept or plug in a point.
or
Stat edit
Stat Calc #0 (ExpReg)

Percent Rate: Amount over/under 1
Ex1. $y = 3(1.2)^x$ has a 20% increase
Ex2: $y = 3(0.4)^x$ has a 60% decrease (1-0.4)

- b) Common Bases

- c) Growth/Decay Formulas: $A(t) = P(1 \pm r)^t$ or $A(t) = P(1 \pm r)^{\frac{t}{\text{every}}}$

$A(t)$ = final amount every = growth period
 P = initial amount
 r = rate (% as a decimal)
 t = time (make sure the time periods are the same)

8. Polynomials

- a) Long Division
- b) Synthetic Division (use only the coefficients. Can't use if the factor has a coefficient >1)

MIDTERM REVIEW STUDY GUIDE

- c) Remainder Theorem (plug the value of x into the equation or graph. It's a factor if the remainder is 0)
- d) Write the equation of a polynomial given zeros/multiplicity
- e) End behavior

